ARBITRARY FUNCTION GENERATING CIRCUIT USING A SIMPLE OPERATIONAL ELEMENT AND AN ENCRYPTION METHOD THEREFOR

5   BACKGROUND OF THE INVENTION

1. Field of the Invention

The present invention relates to an apparatus for simulating complex systems at a high rate of speed and also to
10   a method of modulating signals for encryption.

2. Description of the Related Art

Numerical models for describing quantitative changes are a type of arbitrary function generator that produces specific
15   functions based on the parameters provided. The models can be simulated at high speeds with an analog arithmetic circuit and, in fact, were simulated with analog computers in the past. However, these analog arithmetic circuits are rarely used anymore because the circuits have to be rewired for each problem and
20   enormous circuits are required when the problems are of a large scale. Subsequently, wire connections in the analog arithmetic circuits were modified electrically through software, but this analog calculation method is no longer used because integrating complex circuits is extremely difficult.
25   In order to simulate a phenomenon having multiple variables at a high rate of speed, it is advantageous to generate arbitrary functions with an analog arithmetic circuit. For this method

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to be practical, however, it is necessary to programmably generate functions of different types without needing to physically change the wiring of the arithmetic circuit. Further, the circuit must have a simple construction such as RAM that

5 facilitates high integration by repeating simple mask patterns. It is also necessary to minimize the number of components needed to construct the circuit.

A generalized Lotka-Volterra equation can be used in plant growth models or for the dynamics of biological communities and

10 is represented by a differential equation such as the following.

Equation 1
$$\frac{dx_i}{dt} = x_i\left(r_i + \sum_{j=1}^{n} \mu_{ij} x_j\right) \quad (i = 1, 2, \cdots, n)$$

Here, x_i is the size of a population i representing the

15 elements of a system; μ_{ij} is a constant of interaction between the elements; and r_i is an inherent constant for each element representing the growth rate of the population i. When n is sufficiently large, this equation can approximate a positive arbitrary continuous function of an arbitrary precision by

20 varying n and μ_{ij}, it is possible to generate patterns of x_i that change in various ways. Accordingly, in addition to modeling phenomena, this calculation has a wide range of applications as an arbitrary waveform generator. The present invention focuses on the symmetry of this equation to perform high-speed

25 emulation by performing the calculation in hardware or using parallel processing with multiple digital computers.

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SUMMARY OF THE INVENTION

In view of the foregoing, it is an object of the present invention to provide a simple calculation element, and particularly an arbitrary waveform generating circuit or random function generating circuit for solving the generalized Lotka-Volterra equation through an arithmetic circuit employing relatively simple circuit elements. It is another object of the present invention to provide an encryption/modulation method employing the arbitrary function generating circuit.

These objects and others will be attained by an arbitrary function generating circuit employing a simple arithmetic circuit element for calculating the following generalized Lotka-Volterra equation (Equation 1).

Equation 1 $$\frac{dx_i}{dt} = x_i\left(r_i + \sum_{j=1}^{m} \mu_{ij} x_j\right) \quad (i = 1,2,\cdots,n)$$

Here, x_i is the size of a population i representing the elements of a system; μ_{ij} is a constant of interaction between the elements; and r_i is an intrinsic constant for each element representing the growth rate of the population i. The arbitrary function generating circuit includes a plurality n of modules, each having a plurality n of input terminals and one output terminal; and a plurality n of connecting wires including a first connecting wire for connecting the output terminal of the first module to the first input terminal of each module; a second connecting wire for connecting the output terminal of the second module

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to the second input terminal of each module; and continuing in a like manner until the nth connecting wire for connecting the output terminal of the nth module to the nth input terminal of each module.

5   Each module comprises a group of n variable resistors connected to the n input terminals; an output sum connecting wire connecting the output terminals of the variable resistors in order to total their output values; a multiplier having an amplifier for multiplying the sum of the output values by the
10   output value from the corresponding module; and an integrator for integrating the output values.

The generalized Lotka-Volterra equation is converted to Equation 7 below by setting the interaction coefficient μ_{ij} equivalent to the value of the variable resistors in each module.
15   An arbitrary module in the group of modules is designated as the first module to output constant value 1. A fixed value r_i is replaced by the value μ_{ij} in the variable resistors input via the first input terminal of each module by the first connecting wire.

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Equation 7 $$\frac{dx_i}{dt} = x_i \sum_{j=1}^{n} \mu_{ij} x_j \quad (i = 1, \cdots, n)$$

The arithmetic circuit calculates the converted generalized Lotka-Volterra equation by iterating the following
25   process in which the size x_i (i = 1, 2, …, n) of a population i representing the elements comprising the system for generating an arbitrary function is output by the output terminal of each

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of n modules. This output is transferred to a group of input terminals in a group of modules via n input connection wires and totaled by a connection wire.

According to another aspect of the present invention, the arbitrary function generating circuit further includes an interaction constant setting means for programmably changing each value in the group of variable resistors in each module. Alternatively, FET semiconductor element circuits are provided as the variable resistors in each module. The resistance values in the variable resistors are varied externally using control signals.

According to another aspect of the present invention, an arbitrary function generating circuit includes a plurality (n) of modules each having one input/output signal terminal, and one signal bus connecting each of the input/output signal terminals. Each module comprises a frequency synthesizer; a first multiplier for multiplying the output from the frequency synthesizer with the value input from the signal bus via the input/output terminal; a low pass filter for removing the AC component from the value output by the first multiplier; a second multiplier into which the output from the low pass filter is input; an integrator for integrating the output from the second multiplier; a connecting circuit for inputting the value output from the integrator into the second multiplier, such that the second multiplier can multiply this value from the value output by the low pass filter; an oscillator; and a third multiplier connected to the input/output terminal for multiplying the value

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output by the oscillator with the value output from the integrator.

The value x_i ($i = 1, 2, ..., n$) output by the integrator in each module is the number of elements constructing a system for generating an arbitrary waveform function and is multiplied with a carrier wave signal having an angular frequency ω_i generated by the oscillator by the third multiplier. The multiplied value $x_i \sin \omega_i t$ is output from each module to the signal bus; and an addition value e as shown in Equation 8 is generated by multiplexing the output from each module and re-input via the signal bus.

Equation 8 $$e = x_1 \sin \omega_1 t + x_2 \sin \omega_2 t + \cdots + x_n \sin \omega_n t$$

The value output from the frequency synthesizer is set to a voltage W_1 shown in Equation 9 generated by multiplexing the interaction coefficient μ_{ij}.

Equation 9 $$W_i = \mu_{1i} \sin \omega_1 t + \mu_{2i} \sin \omega_2 t + \cdots + \mu_{ni} \sin \omega_n t$$

The addition value e is multiplied by the voltage W_1 in the first multiplier and passed through the low pass filter to obtain the DC component shown in Equation 10.

Equation 10 $$eW_i = \mu_{1i} x_1 + \mu_{2i} x_2 + \cdots + \mu_{ni} x_n$$

This value eW_i is multiplied by the value of x_i output

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by the integrator in the second multiplier and integrated in the integrator to obtain the signal for x_i. The signal x_i is multiplied in the third multiplier by the carrier wave generated by the oscillator to obtain the signal $x_i \sin \omega_i t$. The signal

5   $x_i \sin \omega_i t$ is output onto the signal bus via the input/output terminal; and the process is repeated.

According to another aspect of the present invention, the arbitrary function generating circuit further includes a means for setting the voltage W_i with the frequency synthesizer that

10   is provided either external to the module as an amplifying circuit for extracting signals from the internal oscillator and adding weight to the signal or internal to the module as an independent circuit.

According to another aspect of the present invention, an

15   arbitrary function generating circuit includes a frequency synthesizer that outputs a value W; a first multiplier that receives the output value W as one input value; a first low pass filter for cutting out a first frequency component from the value output from the first multiplier; a second multiplier that

20   receives the value e_4 output from the first low pass filter as one input value; a second low pass filter that removes a second frequency component lower than the first frequency component from the value output from the second multiplier; an adder that receives the output value e_5 as one input value; a delay circuit

25   that delays the output value e_1 and sets the output value e_1 as the second input value to the adder; a first frequency multiplier that multiplies the frequency of the output value

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e_1 and outputs an output value e_2 as the second input value for the second multiplier; and a second frequency multiplier that multiplies the frequency of the output value e_1 and outputs an output value e_3 as the second input value for the first multiplier.

The amplitude of the signal x_i ($i = 1, 2, …, n$) in Equation 7 is expressed by the AC signal $x_i \sin(i\omega_0)$. Here, $i = 1, 2, …, n$. and ω_0 is a basic angular frequency. The signal e_1 output from the adder is added to the total signal x_i to generate a frequency multiplexed signal as shown in Equation 11.

Equation 11 $$e_1 = x_1 \sin(\omega_0)t + x_2 \sin(2\omega_0)t + \cdots + x_n \sin(n\omega_0)t$$

The frequency multiplexed signal e_1 is constantly maintained in a closed loop delayed by the delay circuit only a time sufficiently longer than the period of the base frequency ω_0. The first frequency multiplier multiplies the frequency of the signal e_1 by α ($n \ll \alpha$) and outputs the signal e_2. The second frequency multiplier multiplies the frequency of the signal e_1 by β ($\alpha \ll \beta$) and outputs the signal e_3. The frequency synthesizer generates at once a signal W that multiplexes the interaction coefficient μ_{ij} (i and $j = 1, 2, …, n$) and outputs the signal W. The first multiplier multiplies the signals e_3 and the W. The first low pass filter removes the frequency component greater than a frequency near $\beta \omega_0$ and outputs the following signal e_4. The second multiplier multiplies the signals e_2 and e_4. The second low pass filter removes the frequency component greater than a frequency near $\alpha \omega_0$ and outputs

the following signal e_5 shown by Equation 18.

Equation 18

$$e_5 = x_1\left(\sum_{j=1}^{n} \mu_{1j}x_j\right)\sin(\omega_0 t) + x_2\left(\sum_{j=1}^{n} \mu_{2j}x_j\right)\sin(2\omega_0 t) + \cdots + x_n\left(\sum_{j=1}^{n} \mu_{nj}x_j\right)\sin(n\omega_0 t)$$

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The generated signal e_5, which corresponds to the frequency multiplexed differential signal de_1/dt on the right side of Equation 7, is added to the signal e_1 in the adder to perform the integration of Equation 7.

10   According to another aspect of the present invention, an encryption method using the arbitrary function generating circuit described above sets the initial value $e_1|_{t=0}$ of the frequency multiplexed signal e_1 as the code to be encrypted and the signal W output from the frequency synthesizer as the key

15   code for encryption. A time change pattern of the signal e_1 or the signal $e_1|_{t=T}$ at a time T is encrypted.

According to another aspect of the present invention, the signal W output from the frequency synthesizer is used as the code to be encrypted and the initial value $e_1|_{t=0}$ of the frequency

20   multiplexed signal e_1 is used as the key code for encryption.

BRIEF DESCRIPTION OF THE DRAWINGS

In the drawings:

25   Fig. 1 is a block diagram showing a module of the first embodiment used in a random function generating circuit of the present invention;

Fig. 2 is a block diagram showing the overall schematic of an arithmetic circuit of the first embodiment;

Fig. 3 is a block diagram showing a module of the second embodiment used in a random function generating circuit of the present invention;

Fig. 4 is a block diagram showing the overall schematic of an arithmetic circuit of the second embodiment;

Fig. 5 is a block diagram showing the overall schematic of an arithmetic circuit of the third embodiment having only one module;

Fig. 6 is an explanatory diagram showing a decryption apparatus using the circuit of the present invention;

Fig. 7 is an explanatory diagram showing paths indicating changes in the value of x_i over time on a plane formed by the two module outputs; and

Fig. 8 is an explanatory diagram showing a public key encryption method using the system of the present invention.

DESCRIPTION OF THE PREFERRED EMBODIMENTS

An arbitrary function generating circuit according to preferred embodiments of the present invention will be described while referring to the accompanying drawings. A first embodiment will be described with reference to Figs. 1 and 2. Fig. 2 shows an overall schematic for an arithmetic circuit of a generalized Lotka-Volterra equation, while Fig. 1 is a block diagram of a module in that circuit.

Here, M_i represents an arbitrary module. The arithmetic circuit is configured of n number of modules. Each module has n number of input terminals P_{ij} and one output terminal Q_i.

The arithmetic circuit further comprises a first connecting wire for connecting the output terminal Q_1 of the first module M_1 to the first input terminals P_{11}, P_{21}, ..., P_{n1} of each module; a second connecting wire for connecting the output terminal Q_2 of the second module M_2 to the second input terminals P_{12}, P_{22}, ..., P_{n2} of each module; and continuing in this way to an nth connecting wire for connecting the output terminal Q_n of the nth module M_n to the nth input terminal P_{1n}, P_{2n}, ..., P_{nn} of each module.

Each module further comprises n input terminals P_{ij}, n variable resistors V_{ij} connected to the corresponding input terminals P_{ij}, connecting wires that add up the outputs from each of the variable resistors V_{ij}, an amplifier A for amplifying the these totaled values, a multiplier T for multiplying the totaled value with the module output value, and an integrator S for integrating this output.

The generalized Lotka-Volterra equation can be computed by connecting arbitrary modules M_i of Fig. 1 in the configuration shown in Fig. 2. Here, we will assume that an interaction coefficient μ_{ij} is equivalent to the value of the variable resistors V_{ij} in each module and that one special module that outputs a fixed value is provided such that r_1 is the input value. Accordingly, Equation 1 can be rewritten as follows.

Equation 2

$$\frac{dx_i}{dt} = x_i\left(r_i + \mu_{i1}x_1 + \sum_{j=2}^{m} \mu_{ij}x_j\right) \quad (i = 1,2,\cdots,n)$$

If the first module M_1 is a fixed output module that always outputs the value $x_1 = 1$, then we have the following.

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Equation 3

$$\frac{dx_i}{dt} = x_i\left(r_i + \mu_{i1}x_1 + \sum_{j=2}^{m} \mu_{ij}x_j\right) \quad (i = 2,3,\cdots,n)$$

Such that,

10   Equation 4 $x_i = 1$

Here, r_i provides a fixed value (biased value) in the parentheses on the right side of the equation. If the role of r_i is assumed by the weighted input μ_{i1} from the first module

15   M_1 ($x_1 = 1$), which constantly outputs a fixed value of 1, then by assuming μ_{i1} is equivalent to r_i, the following equation can be formed.

Equation 5

$$\frac{dx_i}{dt} = x_i\left(\mu_{i1}x_1 + \sum_{j=2}^{m} \mu_{ij}x_j\right) \quad (i = 2,3,\cdots,n)$$

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Based on this assumption,

Equation 6 $\mu_{i1} = r_i$

25   By returning the term $\mu_{i1}x_1$ in the parentheses to the Σ on the right side of Equation 5, we have the following equation.

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Equation 7
$$\frac{dx_i}{dt} = x_i \sum_{j=1}^{n} \mu_{ij} x_j \quad (i = 1, \cdots, n)$$

Therefore, by introducing a module with a fixed output, Equation 1 can be simplified to Equation 7. The right side of the equation can be calculated with an adding circuit for performing a sum calculation (configured by the variable resistors V_{ij} [j = 1-n] and the amplifier A in Fig. 1) and a multiplying circuit (the multiplier T in Fig. 1) for multiplying the value x_i by the result of the previous calculation. The values for x_i, when i = 2, 3, …, n, are obtained by integrating this result using an integrating circuit (the integrator S in Fig. 1).

The time change pattern for values of x_i, when i = 2, 3, …, n, can be changed arbitrarily by the value set for the interaction coefficient μ_{ij} (the value set in the variable resistors V_{ij} [j = 1-n] in Fig. 1). Therefore, the circuit connecting n number of modules M_i in Fig. 1 can be used as an n-1 channel arbitrary function generator. The value of μ_{ij} of the V_{ij} can be varied externally using an element such as a field effect transistor (FET).

This circuit can generate functions having considerable complexity with several to several tens of modules. As the number of elements, or n in Equation 7, becomes large, the number of connections increases on the order n^2, making integration difficult. An additional complex circuit must be provided separately to control the value μ_{ij} of the V_{ij} externally.

Next, a second embodiment of the present invention will

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be described with reference to Figs. 3 and 4. Fig. 4 shows the overall schematic of an arithmetic circuit for the generalized Lotka-Volterra equation, while Fig. 3 is a block diagram of the circuit modules in that arithmetic circuit. Here, N_i represents

5 an arbitrary module. The arithmetic circuit is configured of n number of modules. Each module has one input/output terminal R_i. The input/output terminal R_i for each module is connected to one signal bus line.

Each arbitrary module N_i includes a frequency synthesizer

10 F1; a first multiplier T1 for multiplying the output from the frequency synthesizer F1 with the value input from the signal bus line via the input/output terminal R_i; a low pass filter L for removing the AC component from the value output from the first multiplier T1; a second multiplier T2 into which the output

15 from the low pass filter L is input; an integrator S1 for integrating the output from the second multiplier T2; a connecting circuit for inputting the value output from the integrator S1 into the second multiplier T2, enabling the second multiplier T2 to multiply this value from the value output from

20 the low pass filter L; an oscillator G; and a third multiplier T3 connected to the input/output terminal R_i for multiplying the value output from the oscillator G with the value output from the integrator S1.

When n is large, the input/output of the input/output

25 terminals R_i in the arbitrary modules N_i shown in Fig. 3 are set to sine waves of differing frequency (the amplitude is set as the output value), and signal transfer is performed using

frequency multiplexing. With this method, all signals can be transferred over one connection line (signal bus), achieving interconnection with a single connecting wire, as shown in Fig. 4. In other words, by setting the output value of the arbitrary module N_i to $x_1 \sin \omega_i t$. Signals from each arbitrary module N_i are added to one connecting wire. Accordingly, the voltage of the connecting wire is calculated as follows.

Equation 8 $e = x_1 \sin \omega_1 t + x_2 \sin \omega_2 t + \cdots + x_n \sin \omega_n t$

The interaction coefficient μ_{ij} is similarly expressed by an AC signal. Accordingly, an interaction constant is supplied to the x_i as the following voltage.

Equation 9 $W_i = \mu_{1i} \sin \omega_1 t + \mu_{2i} \sin \omega_2 t + \cdots + \mu_{ni} \sin \omega_n t$

This is generated independently by the frequency synthesizer F1 provided internally in each arbitrary module N_i or externally. The frequency synthesizer F1 can be an amplifying circuit that adds weight to the signal output from the oscillator G disposed inside each module or can be provided in the module shown in Fig. 3 as a completely independent circuit in order to eliminate all problems of phase deviation.

With the configuration of the arbitrary module N_i shown in Fig. 3, the first multiplier T1 generates a signal by multiplying e by W_i. This multiplied signal contains a DC component (a component that changes slower than the carrier wave

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sinω_1t) and an AC component (the frequency being the sum and product of each carrier wave frequency). The DC component of this signal is obtained when the signal passes through the low pass filter L, as follows.

Equation 10 $$eW_i = \mu_{1i} x_1 + \mu_{2i} x_2 + \cdots + \mu_{ni} x_n$$

The sum on the right side of Equation 10 is obtained in real-time. The second multiplier T2 multiplies the value of x_i with this signal and outputs the result, which is the value on the right side of Equation 7. The integrator S1 integrates this signal to obtain the signal for x_i. Next, the third multiplier T3 multiplies the signal x_i with a carrier wave sin ω_it signal generated by the oscillator G to generate an $x_i$sin ω_it signal. This resulting signal is simultaneously input into the first multiplier T1 and output externally via the input/output terminal R_i.

In this way, a calculation equivalent to the generalized Lotka-Volterra equation can be performed by connecting multiple modules N_i by a single signal wire, as shown in Fig. 4.

A method for decreasing the number of connecting wires using different frequencies is a basic technology in analog multiplex communications. Reports for the hardware of neural networks (learning threshold elements) has already been published (Hirokazu Yokoi and Masao Saito, 1986; *New Learning Elements—Foulethret; IEICE Transactions*, Vol. J69-A, No. 6, pp.1173-1175).

The second circuit type in the second embodiment of the present invention is novel in that it greatly reduces through signal frequency multiplexing the number of wires between modules necessary for calculating the generalized Lotka-Volterra equation in a circuit. While the number of wires in the circuit of the first embodiment increases on the order of n^2, that in the circuit of the second embodiment increases on the order of n.

In the circuit shown in Fig. 4, n number of modules is sufficient to calculate a generalized Lotka-Volterra equation having n elements. Since a more complex function can be expressed with a larger number n of modules, it is desirable to reduce as much as possible the number of overall components and wires required for mounting. According to the next method, a generalized Lotka-Volterra equation of an arbitrary scale (an arbitrary n) can be calculated with only one module.

Fig. 5 shows the third embodiment of the present invention. Fig. 5 is a block diagram showing the overall schematic of the arithmetic circuit for the generalized Lotka-Volterra equation achieved in one module.

The module comprises a frequency synthesizer F2 that outputs a value W; a first multiplier T4 that receives the output value W as one input value; a first low pass filter L1 for cutting out the first frequency component from the value output from the first multiplier T4; a second multiplier T5 that receives the value e_4 output from the first low pass filter L1 as one input value; a second low pass filter L2 that removes a second

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frequency component lower than the first frequency component from the value output from the second multiplier T5; an adder B that receives the output value e_5 as one input value; a delay circuit V that delays the output value e_1 and sets the output value e_1 as the second input value to the adder B; a first frequency multiplier H1 that multiplies the frequency of the output value e_1 and outputs an output value e_2 as the second input value for the second multiplier T5; and a second frequency multiplier H2 that multiplies the frequency of the output value e_1 and outputs an output value e_3 as the second input value for the first multiplier T4.

By setting a carrier frequency according to a method described later and performing the calculation using the circuit shown in Fig. 5, it is possible to achieve the same effects as the circuit in the second embodiment with fewer components.

The amplitude of the signal x_i, where $i = 1, 2, …, n$, in Equation 7 is expressed by the AC signal $x_i \sin(i\omega_0)$ for $i = 1, 2, …, n$. Here, ω_0 is the basic angular frequency and the value is arbitrary (the value is determined according to the objective and application and the frequency characteristics of the components during actual manufacturing). In other words, x_i is expressed by the strength of the signal having an angular frequency of an integral multiple of ω_0.

All signals can be added and transferred over one signal line, since each AC signal is linearly independent from the others (that is, signal transfer using frequency multiplexing). A frequency multiplexed signal obtained by adding all frequencies

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is shown in the following equation.

Equation 11 $\qquad e_1 = x_1\sin(\omega_0 t)+x_2\sin(2\omega_0 t)+\cdots+x_n\sin(n\omega_0 t)$

5   The frequency multiplexed signal e_1 is set as the input value
of the delay circuit V in Fig. 5.

The e_1 is delayed only a time sufficiently longer than
the period of the base frequency ω_0 ($2\pi/\omega_0$) by the delay circuit
V and is again input into the delay circuit V after passing through

10   the adder B.   In other words, the e_1 is output from the delay
circuit V and returns to the delay circuit V, and is therefore
constantly maintained in this closed loop.

The signal added to e_1 in the adder B is set to the frequency
multiplexed differential signal de_1/dt shown in the following

15   equation.   This differential signal is multiplexed in the same
way as the differential value dx_i/dt defined on the left side
of Equation 7, where i = 1, 2, …, n.

Equation 12 $\qquad \dfrac{de_1}{dt} = \dfrac{dx_1}{dt}\sin(\omega_0 t)+\dfrac{dx_2}{dt}\sin(2\omega_0 t)+\cdots+\dfrac{dx_n}{dt}\sin(n\omega_0 t)$

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Hence, e_1 and de_1/dt are added by the adder B.

Equation 13

$$e_1 + \frac{de_1}{dt} = \left(x_1 + \frac{dx_1}{dt}\right)\sin(\omega_0 t)+\left(x_2 + \frac{dx_2}{dt}\right)\sin(2\omega_0 t)+\cdots+\left(x_n + \frac{dx_n}{dt}\right)\sin(n\omega_0 t)$$

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Since this addition equation is exactly the integral
calculation performed according to the Euler method, the integral

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calculation of Equation 7 is achieved by a closed loop circuit formed by the adder B and delay circuit V.

A major issue is how to construct the frequency multiplexed differential signal de_1/dt with a simple circuit. The present invention solves this problem by multiplying two signals having differing frequencies and twice making use of the phenomenon in which a beat signal corresponding to the differential frequency between the two is generated, as described below.

The first frequency multiplier H1 multiplies the frequency of the signal e_1 by α ($n \ll \alpha$) and outputs the signal e_2.

Equation 14
$$e_2 = x_1\sin(\alpha\omega_0)t + x_2\sin(2\alpha\omega_0)t + \cdots + x_n\sin(n\alpha\omega_0)t$$

Similarly, the second frequency multiplier H2 multiplies the frequency of the signal e_1 by β ($\alpha \ll \beta$) and outputs the signal e_3.

Equation 15
$$e_3 = x_1\sin(\beta\omega_0)t + x_2\sin(2\beta\omega_0)t + \cdots + x_n\sin(n\beta\omega_0)t$$

The frequency synthesizer F2 generates at once a signal W that multiplexes the interaction coefficient μ_{ij}, such that i and j = 1, 2, …, n, as follows, and outputs the signal W.

Equation 16

$$W = \mu_{11}\sin(\beta\omega_0 + \alpha\omega_0 + \omega_0)t + \mu_{12}\sin(2\beta\omega_0 + \alpha\omega_0 + \omega_0)t + \cdots + \mu_{1n}\sin(n\beta\omega_0 + \alpha\omega_0 + \omega_0)t$$
$$+ \mu_{21}\sin(\beta\omega_0 + 2\alpha\omega_0 + 2\omega_0)t + \mu_{22}\sin(2\beta\omega_0 + 2\alpha\omega_0 + 2\omega_0)t + \cdots + \mu_{2n}\sin(n\beta\omega_0 + 2\alpha\omega_0 + 2\omega_0)t$$
$$\mathbf{M}$$
$$+ \mu_{n1}\sin(\beta\omega_0 + n\alpha\omega_0 + n\omega_0)t + \mu_{n2}\sin(2\beta\omega_0 + n\alpha\omega_0 + n\omega_0)t + \cdots + \mu_{nn}\sin(n\beta\omega_0 + n\alpha\omega_0 + n\omega_0)t$$

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With the construction described above, the first multiplier T4 first multiplies the e_3 and the W generated by the frequency synthesizer F2 to generate a signal comprising the sum frequency and difference frequency of an AC signal that includes e_3 and W. The first low pass filter L1 removes the frequency component greater than a frequency near $\beta \omega_0$ and outputs the following signal e_4.

Equation 17

$$e_4 = \left(\sum_{j=1}^{n} \mu_{1j}x_j\right)\sin(\alpha\omega_0 + \omega_0) + \left(\sum_{j=1}^{n} \mu_{2j}x_j\right)\sin(2\alpha\omega_0 + 2\omega_0) + \cdots + \left(\sum_{j=1}^{n} \mu_{nj}x_j\right)\sin(n\alpha\omega_0 + n\omega_0)$$

Next, the second multiplier T5 multiplies e_2 and e_4. The second low pass filter L2 removes the frequency component greater than a frequency near $\alpha \omega_0$ and outputs the following signal e_5.

Equation 18

$$e_5 = x_1\left(\sum_{j=1}^{n} \mu_{1j}x_j\right)\sin(\omega_0) + x_2\left(\sum_{j=1}^{n} \mu_{2j}x_j\right)\sin(2\omega_0) + \cdots + x_n\left(\sum_{j=1}^{n} \mu_{nj}x_j\right)\sin(n\omega_0)$$

This equation expresses the right side of Equation 2 that is multiplexed. In other words, this equation corresponds to the multiplexed differential signal de_1/dt.

The signal e_5 (de_1/dt) is added to the signal e_1 that has passed through the delay circuit V by the adder B, thereby integrating Equation 2 by the method described above.

This method theoretically enables Equation 7 to be calculated for an arbitrary n using only one circuit shown in Fig. 5. Due to the difference in initial values of $l_i|_{t=0}$, and

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the signal W in Equation 16 in the circuits of Figs. 5, l_i demonstrates various differing time change patterns. Accordingly, by interpreting $l_i|_{t=0}$ as the value to be encoded (modulated) and W as the key code for encryption, then the time change pattern of l_i or the signal $l_i|_{t=T}$ in time T can be used as the signal to be encoded (modulated). It is also possible to assume the opposite, that is, that W is the value to be encoded (modulated) and $l_i|_{t=0}$ is the key code for encryption.

As described above, it is possible to encode or modulate signals using the arithmetic circuits of Figs. 5. It is also possible to decode or demodulate the encoded signals to the original signal according to a key code using the same arithmetic circuits.

Next, the signal decryption method will be described in greater detail.

Fig. 6 shows an example configuration of a decryption apparatus 60 used for decoding encoded signals. x_i can be various functions depending on the value set for the interaction coefficient μ_{ij}, such that i and j = 1, 2, 3, …, n, and the initial value of x_i, such that i = 1, 2, 3, …, n. Encryption uses this property as described below.

The output values of n units are variables in which n-1 variables change according to time, while one unit outputs a fixed value. For purposes of simplifying the description, we will choose two variables x_k and x_l and consider a path traveled by a point p at the coordinates x_k and x_l in the plane passing through these two variables (see Fig. 7). According to the work

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of the arbitrary function generation of the circuit, the path of the point p moves in an extremely large variety of patterns from an initial value A Point. Here we will assume that the interaction coefficient μ_{ij}, such that i and j = 1, 2, 3, …,

5   n, converges at a point 1 when starting from the initial value A Point after describing a spiral path and converges at a point 0 when starting from initial points B and C. We will further assume that the points of convergence are only these two points 1 and 0. Accordingly, the transmitter can safely transmit

10   one-bit data indicating 1 or 0.

Hence, the transmitter can send a signal corresponding to the point A when wishing to send the data "1" safely and a signal corresponding to the point B when wishing to send the data "0." The receiver can accurately learn the data at the

15   convergence point by applying the previously prepared interaction coefficient μ_{ij} to the decryption apparatus 60. For example, when the transmitter sends data for the point A, the receiver inputs data for the point A and data for the interaction coefficient μ_{ij} into the decryption apparatus 60 to accurately

20   learn that the convergence point is 1.

Since the combinations of the interaction coefficient μ_{ij} are nearly infinite, it is nearly impossible for someone unaware of the true value of the interaction coefficient to guess the interaction coefficient μ_{ij} from the transmitted data.

25   Accordingly, it would be extremely difficult to decode data that has been encoded by the decryption apparatus 60.

Next, the method of encoding the signals with an encryption

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apparatus will be described in more detail.

When not using a public key (interaction coefficient μ_{1j})

The process below is followed in order to encode data equivalent to the point 1.

5 (1) An initial value is generated arbitrarily. If the value converges to the point 1 in the encryption apparatus, that initial value is used as the encoded value. If, however, the initial value converges at point 0, that initial value is discarded and another initial value is generated arbitrarily.

10 (2) Step (1) is repeated until an initial value that converges at point 1 is obtained. The procedure for encoding a value corresponding to the point 0 can be performed according to the same method.

When using a partially public key

15 When transferring encoded credit card numbers for mail orders and the like, it is necessary to transfer a key for the encryption by mail. This is highly inconvenient. Therefore, a public key encryption method is necessary. The conventional method using prime numbers utilizes the fact that an extremely

20 large method would be required to factor out prime factors from large numbers. Accordingly, the method is flawed in that security drops abruptly with improvements in computer performance and the development of efficient prime factorization algorithms. The method described below encodes while

25 performing simulation using analog operations, and therefore has extremely tight security, since the amount of calculations required for a third party to decode the data is nearly infinite.

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The procedure for performing encoded data transfers by a public key encryption using the encryption apparatus is described below.

Preparations

A group of n units forming the present apparatus is divided into an A group and a B group. The A group is a group of units for the encryption apparatus possessed by the encoder and transmitter. The B group is a group of units for the decryption apparatus possessed by the decoder. Most of the interaction coefficient μ_{ij} between the A and B groups of units are 0, while only a specific interaction coefficient is a value other than 0. Only some of the units in the B group are connected by an interaction coefficient other than 0 to the A group and affect the B group. This group is called the C group. Similarly, a portion of units in the A group are connected to the B group by an interaction coefficient other than 0 and affect the A group. This group is called the D group.

For simplicity, let us assume that the interaction coefficients are set to have only two convergence points, such that the output values x_k, x_l, x_a, and x_b from four units have two convergence points in a four-dimensional area. The units k and l outputting the variables x_k and x_l belong to the A group (however, the output values do not belong in the public C group) and the units a and b outputting the variables x_a and x_b belong to the B group (however, their output values do not belong in the public D group). The convergence point in the plane of variables x_k and x_l has a one-on-one correspondence with the convergence point in the plane of variables x_a and x_b. The

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interaction coefficient and growth rate (fixed parameter r_i) are preset to enable estimation of the convergence point in the plane of x_k and x_l from the convergence point from the plane of x_a and x_b.

5   While the transmitter only possesses data concerning the A group, the transmitter can dynamically extract data regarding the D group from the receiver to perform calculations for the A group units. In other words, the transmitter can simulate (calculate) movement of the coordinates (x_k, x_l) from data on

10   the A group and D group. Similarly, the receiver can simulate movement of the coordinates (x_a, x_b) from data concerning the B and C groups.

Public key data

To encode and transmit data, the transmitter acquires data

15   of the interaction coefficient μ_{ij} and fixed parameter r_i for the A group made public by the receiver and acquires of data of the output value x_i for the C group (i being the unit number of the C group) as unencrypted data. Using this data, the transmitter performs a simulation of the A group.

20   Encryption   accompanying   normal   interactive communications

Since output values from the C group vary during the simulation, the transmitter simulates the A group while receiving unencrypted output values for the C group in real-time, in order

25   to simulate the A group. At the same time, the receiver simulates the B group while receiving unencrypted data for the D group from the transmitter in real-time. In other words, the receiver

and transmitter exchange unencrypted data on the D and C groups in real-time, while the transmitter simulates the A group and the receiver simulates the B group independently. It is obvious that a third party cannot participate in this interactive communication.

Data that the transmitter wishes to send encrypted and the initial values of the A group are not known to the receiver or a third party. The receiver can estimate data concerning the convergence value of the A group from position data for the convergence point in the B group simulation. However, a third party cannot simulate either the A or B groups because the third party does not possess the initial values for the A group or data for the B group. Accordingly, a third party cannot decode the encrypted data.

The arbitrary function generating circuit according to the present invention constructed of a simple calculation element and the encryption/modulation method using this circuit demonstrates the following effects.

(1) The present invention is a high-speed processing device for performing simulations. That is, the present invention can be used to perform high-speed simulations of a generalized Lotka-Volterra equation, which is employed as a complex and dynamic biological model for simulating such processes as changes in the number of species in a biosystem and the growth of plants. The arbitrary m function generating function of the present invention can be applied to a general simulator for such complex systems as market conditions and economic fluctuations and has

a wide range of applications as a high-speed simulator for complex systems.

(2) The present invention can be used as an apparatus for generating complex waveforms. Accordingly, extremely complex waveforms can be generated with a relatively simple circuit simply by changing a small portion of the circuit parameters slightly, it is possible to create various waveforms. Since periodic or aperiodic waveforms can be generated according to the parameters, the invention can be used as a sound generator for electronic instruments or game machines. Further, since a slight change in parameters can generate irregular waveforms, the present invention can also apply to warning sirens and the like for preventing the threat of harmful pests.

(3) The present invention can apply to an encryption apparatus. A generalized Lotka-Volterra equation has a plurality of equilibrium points according to the parameters and converges at different equilibrium points depending on the initial value. The set of initial values is infinite while the number of equilibrium points is finite. Therefore, data for secure transfer is encrypted as position data of a equilibrium point. When the transmitter sends the data, one initial value from the set of initial values that converge at this equilibrium point is arbitrarily selected. Using a circuit with the same parameter values, the receiver can find the convergence point. However, it is nearly impossible for a third party to decode the message without knowledge of these parameters. Accordingly, the present invention can be applied to an encryption apparatus for

high-speed and extremely secure data transfer.

(4) The present invention can apply to a pattern recognition apparatus. Using a circuit having the same plurality of equilibrium points as the encryption apparatus described above, an initial value vector is set to the input pattern and a converging point is set to the recognition result. By establishing appropriate parameters in advance, the present invention can therefore be applied to a high-speed pattern recognition apparatus. Existing nonlinear optimal algorithms can be used to determine appropriate parameters.

(5) The present invention can be used for encryption and decryption signals in spread spectrum communications. A circuit having a plurality of equilibrium points describes a certain path before arriving at the equilibrium point. This type of nonlinear system possesses robustness in achieving the same equilibrium point, even though a certain level of noise is generally introduced into the signal. The larger value n, the more robust the system is to noise. Accordingly, the circuit types 2 and 3 described in embodiments 2 and 3, respectively, having an n as large as possible are most appropriate.

The output from the third multiplier of the type 2 and the output from the second frequency multiplier of the third circuit type have an extremely broad spectrum from the low frequency to high frequency range. After modulation, this signal can be transmitted in a transmission wave having an extremely broad band. The demodulated signal is input into a circuit on the receiving end having the same circuit constant

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and the same components as those on the transmitting end (output from the third multiplier in the type 2 and output from the second frequency multiplier in the type 3). The receiver can therefore obtain correct data, providing the noise introduced into the

5 signal is not large, since the signal describes the same path as that for the transmitter and reaches the correct equilibrium point. Even if the demodulated signal contains a large amount of noise, converging on atractor point will increase the percentage of the signal reaching the same equilibrium point

10 as the transmitters. This percentage is greater with a larger n.